

## 3.3 - Equations With Variables on Both Sides

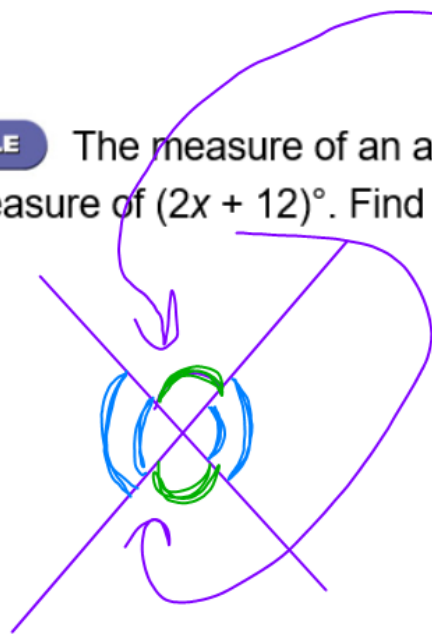
Vocabulary:

identity -

$$3 \cdot 1 = 3$$

$$2x + 9 = 2x + 9$$

**1 EXAMPLE** The measure of an angle is  $(5x - 3)^\circ$ . Its vertical angle has a measure of  $(2x + 12)^\circ$ . Find the value of  $x$ .



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$$\begin{array}{r} 5x - 3 \neq 2x + 12 \\ -2x \quad \downarrow -2x \end{array}$$

$$\begin{array}{r} 3x - 3 \neq 12 \\ +3 \quad \downarrow +3 \end{array}$$

$$3x = 15$$

$$x = 5$$

**Solve each equation. Check your answer.**

$$1. \quad 6x - 2 = x + 13$$

*(Handwritten: -x, ↓x)*

$$5x - 2 = 13$$

*(Handwritten: +2, +2)*

$$5x = 15$$

$$x = 3$$

$$2. \quad 5y - 3 = 2y + 12$$

*(Handwritten: -2y, ↓2y)*

$$3y - 3 = 12$$

*(Handwritten: +3, +3)*

$$3y = 15$$

$$y = 5$$

**2 EXAMPLE** You can buy a skateboard for \$60 from a friend and rent the safety equipment for \$1.50 per hour. Or you can rent all items you need for \$5.50 per hour. How many hours must you use a skateboard to justify buying your friend's skateboard?

$$\begin{array}{r} 60 + 1.5h \\ - 1.5h \\ \hline 60 \end{array} = \begin{array}{r} 5.5h \\ - 1.5h \\ \hline 4h \end{array}$$

$$\frac{60}{4} = \frac{4h}{4}$$

$$\boxed{15 = h}$$

hours

- 11. Telephone Service** One telephone company charges \$16.95 per month and \$0.05 per minute for local calls. Another company charges \$22.95 per month and \$0.02 per minute for local calls. For what number of minutes of local calls per month is the cost of the plans the same?

$$16.95 + 0.05m = 22.95 + 0.02m$$

$$16.95 + 0.03m = 22.95$$

$$\frac{0.03m}{0.03} = \frac{6}{0.03}$$

$$m = 200 \text{ minutes}$$

**3** **EXAMPLE** Solve  $2.5x \pm 1 \neq 4x - 2.6$  using a graphing calculator.

$$13. 7(3 - k) = -3k + 4$$

$$21 - 7k = -3k + 4$$

$$+7k \quad +7k$$

$$21 = 4k + 4$$

$$-4 \quad -4$$

$$\frac{17}{4} = \frac{4k}{4}$$

$$\boxed{4\frac{1}{4} = k}$$

**4 EXAMPLE** Solve each equation.

a.

$$4 - 4y = -2(2y - 2)$$

$$4 - 4y = -4y + 4$$

identity

$$4 = 4$$

b.

$$-6z + 8 = z + 10 - 7z$$

$$-6z + 8 = -6z + 10$$

$$8 \neq 10$$

NO SOLUTION



$$19. \cancel{6x} + 1 = \cancel{6x} - 8 \quad \text{NO solution}$$

$$21. y - 5 = -1(5 - y) \\ = -5 + y$$

identity

HW: pg. 137 #7, 10, 12, 21, 25, 31,  
33, 37, 48, 57